

Charge Instability in Quadrupolar Chromophores: Symmetry Breaking and Solvatochromism

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Abstract: We present a joint theoretical and experimental work aimed to understand the spectroscopic behavior of multipolar dyes of interest for nonlinear optics (NLO) applications. In particular, we focus on the occurrence of broken-symmetry states in quadrupolar organic dyes and their spectroscopic consequences. To gain a unified description, we have developed a model based on a few-state description of the charge-transfer processes characterizing the low-energy physics of these systems. The model takes into account the coupling between electrons and slow degrees of freedom, namely, molecular vibrations and polar solvation coordinates. We predict the occurrence of symmetry breaking in either the ground or first excited state. In this respect, quadrupolar chromophores are classified in three different classes, with distinctively different spectroscopic behavior. Cases of true and false symmetry breaking are discriminated and discussed by making resort to nonadiabatic calculations. The theoretical model is applied to three representative quadrupolar chromophores: their qualitatively different solvatochromic properties are connected to the presence or absence of broken-symmetry states and related to two-photon absorption (TPA) cross-sections. The proposed approach provides useful guidelines for the synthesis of dyes for TPA application and represents a general and unifying reference frame to understand energy-transfer processes in multipolar molecular systems, offering important clues to understand basic properties of materials of interest for NLO and energy-harvesting applications.

Introduction

Charge resonance is a characteristic feature of organic molecules where electron donor (D) and acceptor (A) groups are linked by π -conjugated bridges. Charge transfer between D and A groups characterizes the low-energy physics of these molecules and is responsible for the appearance of low-energy excitations with large transition and/or mesomeric dipole moments.^{1–3} Dipolar (D- π -A),^{1–5} quadrupolar (D- π -A- π -D or A- π -D- π -A),^{6–13} or more generally, multipolar molecules^{14–18}

are therefore extensively investigated for applications in nonlinear optics (NLO). At the same time, because the low-energy excitations in these dyes imply large charge displacements, their linear and nonlinear optical spectra are strongly affected by the

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surrounding medium: dipolar and multipolar dyes with strong NLO responses are often good polarity probes.^{2,17,19,20} The charge resonance implies a rearrangement of the electronic distribution in the molecule, with important consequences on bond orders and hence on the molecular geometry: vibrational and electronic degrees of freedom are strongly coupled, leading to important spectroscopic effects,^{20–23} as well as large vibrational contributions to NLO responses.^{3,24–26} Charge resonance is also the fundamental process in charge-transfer complexes and salts,^{27,28} i.e., systems where the charge-transfer interaction occurs between electron-donor and -acceptor molecules, and in mixed-valence metallic complexes and chains, where electrons hop between metallic ions kept together by ligand groups.²⁹ Charge and structural instabilities and symmetry-breaking phenomena have been quite extensively investigated in these systems as a consequence of electron-vibration coupling.^{30–32}

Here, we propose the occurrence of similar phenomena in multipolar organic dyes.

A large body of experimental data is available for many families of quadrupolar^{5,7,9–11,13,18,33–36} and octupolar^{15,17,18,34,37–45} chromophores as well as for branched and dendritic systems.^{16,40,43,44,46,47} Because of their highly symmetric structure, all of these systems have no permanent dipole moment and, of course, vertical (unrelaxed) states are nondipolar as well. However, for many of these chromophores, experimental data suggest the existence of polar excited states. For example, strong fluorescence solvatochromism has been observed for quadrupolar and/or octupolar systems,^{10,13,17,18,36,42,48,49} revealing the existence of highly dipolar excited states. Time-resolved fluorescence anisotropy measurements suggest that the initially delocalized excitation may localize in the picosecond time scale over one branch of the chromophore, leading to the formation of a polar state.^{38,44} Recent electroabsorption measurements^{40,41} also point to the formation of dipolar excited states in 3-fold symmetric systems. The interpretation of this behavior is still

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controversial: quadrupolar (or multipolar) solvation has been proposed as responsible for the fluorescence solvatochromism;¹³ localization or delocalization of excitations is a hotly debated topic for dendrons and branched compounds in general;^{18,34,38,39,43–45,47} and the interpretation of electroabsorption measurements is delicate and invokes structural disorder to explain the dipolar nature of the vertical excited state.^{40,41}

In this paper, we propose a general model for multipolar chromophores in solution and apply it specifically to quadrupolar systems. The model, on the basis of an essential-state description for the electronic system, accounts for electron-vibration coupling and solvation effects. A detailed and internally consistent description of the ground state and the (spectroscopically relevant) low-lying excited states is obtained in terms of the corresponding potential energy surfaces (PES). Multistable behavior shows up with multiple-minima PES. We investigate in detail the occurrence of charge instabilities and relaxation in either the ground or excited states. Full nonadiabatic diagonalization is adopted as a powerful and flexible computational tool for the simulation of linear and nonlinear optical spectra. The approach is general and will be described in full detail in a forthcoming paper. Here, we present the main features of the model for quadrupolar DAD or ADA chromophores and validate it through an extensive comparison with experimental data. To such an aim, a couple of chromophores have been synthesized and fully characterized to provide stringent tests for the proposed model.

In the next section, we shortly introduce the model and show that, depending upon the charge distribution on the molecule, bistable solutions can be expected in either the ground or the excited one-photon allowed states. Symmetry breaking and hence the dipolar nature of these states is then frozen because of the coupling to slow (vibrational and solvation) degrees of freedom. Spectroscopic consequences of symmetry breaking are discussed, with special emphasis on absorption and/or fluorescence solvatochromism. The model is then validated against experiments. We present experimental data collected in solution for a newly synthesized fluorene-based chromophore that shows large two-photon absorption (TPA) and solvent-independent one-photon absorption (OPA) spectra and a strongly solvatochromic fluorescence. This complex spectroscopic behavior is naturally explained by the proposed model. A similar behavior was indeed observed for other quadrupolar dyes, and the model is further validated by the comparison with published data on a different dye based on a tetrafluorobenzene ring as the central A group. Finally, the case of a squaraine-based quadrupolar dye is discussed. We collect linear and nonlinear spectra of this dye that barely shows no solvatochromism. This markedly different behavior is naturally described within the proposed model. The model offers a microscopic picture for symmetry breaking in multipolar chromophores and rationalizes in a unifying reference scheme their variegated spectroscopic behavior. A classification of quadrupolar dyes emerges from this picture, offering a useful design tool for the synthesis of chromophores with desired properties.

Bistability and Symmetry Breaking: Model and Concepts

Charge resonance in D- π -A- π -D chromophores is described in chemical language as the resonance among three structures:

D⁺A⁻D \leftrightarrow DAD \leftrightarrow DA⁻D⁺ (here and hereafter, we will explicitly refer to D- π -A- π -D structures, but the same discussion applies to A- π -D- π -A chromophores, provided that the role of D and A is interchanged). These states dominate the low-energy physics of the chromophores and suggest the use of a three-state picture to describe their electronic structure: indeed, a three-state model has already been successfully adopted to describe quadrupolar donor-acceptor-based compounds for NLO applications and to optimize their TPA cross-section.^{50,51} However, the solvatochromism of quadrupolar dyes was not addressed in these papers. Here, for the first time, we extend the three-state electronic model to account at the same time for electron-vibration coupling and solvation effects. In the spirit of the Mulliken model²⁷ that has been successfully applied to describe polar, D- π -A, chromophores (also known as push-pull chromophores),^{20,21,25,52} the charge resonance model for quadrupolar chromophores is written on the basis of a set of three orthogonal states: $|N\rangle$, the neutral state, corresponding to the DAD structure, and two degenerate states, $|Z_1\rangle$ and $|Z_2\rangle$, corresponding to the two zwitterionic structures D⁺A⁻D and DA⁻D⁺, respectively. We define 2η as the energy difference between the two degenerate zwitterionic states and the neutral state, so that for positive η the neutral form is lower in energy than the zwitterionic forms, whereas the opposite occurs for negative η . The mixing between the states is described by an off-diagonal matrix element in the Hamiltonian, $\langle N|H|Z_1\rangle = \langle N|H|Z_2\rangle = -\sqrt{2}t$, that measures the probability of electron transfer from D to A and backward. The direct mixing between Z_1 and Z_2 is set to 0, because it implies the direct hopping between non-nearest neighbor sites. The dipole moments associated with the two zwitterionic states point in opposite directions but have the same magnitude, μ_0 , that is by far the largest matrix element of the dipole moment operator in the chosen basis: all other matrix elements of the dipole moment operator will be accordingly disregarded.

By exploiting inversion symmetry, we combine the zwitterionic states in symmetric and antisymmetric wavefunctions: $|Z_+\rangle = 1/\sqrt{2}(|Z_1\rangle + |Z_2\rangle)$ and $|Z_-\rangle = 1/\sqrt{2}(|Z_1\rangle - |Z_2\rangle)$, respectively. The N state is even, so that it only mixes to $|Z_+\rangle$. On the symmetrized basis (N , $|Z_+\rangle$, and $|Z_-\rangle$), the following three operators are conveniently defined:

$$\hat{\rho} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \hat{\delta} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \quad \hat{\sigma} = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad (1)$$

Here, $\hat{\sigma}$ mixes the two *gerade* states; the two operators $\hat{\rho}$ and $\hat{\delta}$ define the charge distribution in the molecule; $\hat{\rho} = \hat{\rho}_1 + \hat{\rho}_2$ measures the average charge on the central A site, sum of the charges on the two external D sites; $\hat{\delta} = \hat{\rho}_1 - \hat{\rho}_2$ instead measures the unbalance of the charge on the two external (D) sites. In terms of these operators, the representative matrices of the Hamiltonian and dipole moment operators are

$$H_{\text{el}} = 2\eta\hat{\rho} - 2t\hat{\sigma}, \quad \hat{\mu} = \mu_0\hat{\delta} \quad (2)$$

The eigenstates of the Hamiltonian are easily obtained as

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$$\begin{aligned}
 |g\rangle &= \sqrt{1-\rho}|N\rangle + \sqrt{\rho}|Z_+\rangle \\
 |c\rangle &= |Z_-\rangle \\
 |e\rangle &= \sqrt{\rho}|N\rangle - \sqrt{1-\rho}|Z_+\rangle
 \end{aligned}
 \quad (3)$$

where ρ , the ground-state expectation value of the $\hat{\rho}$ operator, measures the weight of Z_+ in the ground state. The charge distribution in the ground state then corresponds to $D^{+0.5\rho}A^{-\rho}D^{+0.5\rho}$, so that ρ measures the quadrupolar character of the ground state. This important observable is fixed by the model parameters, as follows:

$$\rho = 0.5(1 - \eta/\sqrt{\eta^2 + 4t^2}) \quad (4)$$

The operator $\hat{\delta}$, proportional to the dipole moment operator, breaks the inversion symmetry and has vanishing expectation values in all states.

Transition energies and dipole moments can be expressed in terms of ρ

$$\begin{aligned}
 \hbar\omega_{gc} &= E_c - E_g = 2t\sqrt{\frac{1-\rho}{\rho}}, \quad \mu_{gc} = \langle g|\hat{\mu}|c\rangle = \mu_0\sqrt{\rho} \\
 \hbar\omega_{ge} &= E_c - E_g = 2t\sqrt{\frac{1}{\rho(1-\rho)}}, \quad \mu_{ge} = \langle g|\hat{\mu}|e\rangle = 0 \\
 \hbar\omega_{ce} &= E_e - E_c = 2t\sqrt{\frac{\rho}{1-\rho}}, \\
 \mu_{ce} &= \langle c|\hat{\mu}|e\rangle = -\mu_0\sqrt{1-\rho}
 \end{aligned}
 \quad (5)$$

The odd c state in eq 3 is one-photon (OP) allowed by symmetry, while the even e state is two-photon (TP) allowed from the ground state and OP allowed from the c state. For large positive η , the ground state is largely dominated by the N state, $\rho \rightarrow 0$, and the OP and TP excitations become degenerate. In the opposite limit of large and negative η , the ground state is zwitterionic ($\rho \rightarrow 1$) and the OP excitation energy goes to 0 (the ground state becomes degenerate), whereas the TP allowed state has a higher energy (-2η). The other notable case is $\eta = 0$, where $\rho = 0.5$, and the c state is located just midway between the g and e states.

The coupling between electronic and vibrational degrees of freedom is related to the different geometry associated with the neutral and zwitterionic states, much as it occurs for polar D- π -A chromophores.²⁵ The charge rearrangement from N to Z_1 or to Z_2 states occurs along the two (left and right) arms of the quadrupolar molecule, so that we introduce two mutually decoupled effective coordinates, q_1 and q_2 , describing the nuclear motion in each arm. The two coordinates are equivalent by symmetry and have the same harmonic frequency, ω . To describe the linear electron-vibration coupling, we introduce a vibrational relaxation energy, ϵ_v , relevant to the two (equivalent) $N \rightarrow Z_1$ or $N \rightarrow Z_2$ processes. The relevant Hamiltonian reads

$$H = H_{el} - \sqrt{2\epsilon_v}\omega q_1\hat{\rho}_1 - \sqrt{2\epsilon_v}\omega q_2\hat{\rho}_2 + \frac{1}{2}(\omega^2 q_1^2 + p_1^2) + \frac{1}{2}(\omega^2 q_2^2 + p_2^2) \quad (6)$$

where p_1 and p_2 are the conjugate momentum operators. By exploiting inversion symmetry, we define the symmetric and antisymmetric coordinates

$$q_+ = \frac{1}{\sqrt{2}}(q_1 + q_2) \quad q_- = \frac{1}{\sqrt{2}}(q_1 - q_2) \quad (7)$$

and conjugate momenta, p_+ and p_- . The Hamiltonian in eq 6 then reads

$$H = H_{el} - \sqrt{\epsilon_v}\omega q_+\hat{\rho} - \sqrt{\epsilon_v}\omega q_-\hat{\delta} + \frac{1}{2}(\omega^2 q_+^2 + p_+^2) + \frac{1}{2}(\omega^2 q_-^2 + p_-^2) \quad (8)$$

From this Hamiltonian, one immediately recognizes the different roles played by the symmetric and antisymmetric vibrations: q_+ is coupled to $\hat{\rho}$, so that oscillations along q_+ modulate the mixing between N and Z_+ and hence the amount of charge transferred in a symmetrical way from D to A. On the opposite, q_- is coupled to the antisymmetric $\hat{\delta}$ operator: oscillations along q_- induce a mixing of the symmetric N and Z_+ states with the antisymmetric Z_- state, driving an unbalance of the charge on the two external sites. In the adiabatic approximation, one neglects the vibrational kinetic energy (terms proportional to squared vibrational momenta, p_+^2 and p_-^2 in eq 8) to define an electronic Hamiltonian where vibrational coordinates enter as classical variables. Because q_- mixes states with different symmetry, Z_- is no longer decoupled and one has to resort to numerical techniques to diagonalize the 3×3 matrix. Diagonalization leads to three eigenstates that, similar to the Hamiltonian, depend upon q_+ and q_- . The corresponding energies, functions of the two vibrational coordinates, define the PES for the nuclear motion and contain all of the information needed to describe optical spectra as well as symmetry-breaking phenomena.

Stable eigenstates with respect to symmetry breaking show a single minimum located at $q_- = 0$ and $q_+ = \sqrt{\epsilon_v}\langle\rho\rangle/\omega$, where $\langle\rho\rangle$ is the expectation value of $\hat{\rho}$ in the relevant state. Unstable eigenstates instead show a double-minimum structure: the symmetrical $q_- = \delta = 0$ solution corresponds to a saddle point in the PES, i.e., to an unstable state. Two equivalent minima at finite and opposite q_- values ($q_- = \pm\sqrt{\epsilon_v}\langle\delta\rangle/\omega$) define two equivalent stable solutions that correspond to broken-symmetry and hence polar states.

Figure 1 shows the relevant phase diagram where systems can be located as a function of ρ , the ground-state quadrupolar moment, and ϵ_v , the strength of electron-vibration coupling. The lines in the phase diagram mark values of the ρ and ϵ_v parameters for which the PES of the ground state (rightmost line) or the PES of the OP excited state (leftmost line) have zero curvature along the q_- coordinate, while the q_+ coordinate is fixed at its equilibrium value for the ground state. These boundaries distinguish three different regions, as schematically shown by the PES sketched in each region. Typical organic chromophores have ϵ_v values on the order of 0.5 or less

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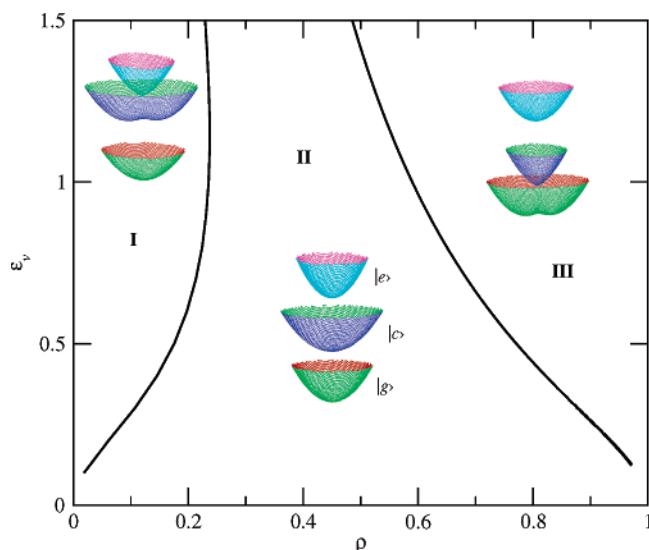


Figure 1. Phase diagram for quadrupolar chromophores, describing the stability of the different states (according to the PES sketched in each region) as a function of ρ (the quadrupolar character) and ϵ_v (the electron-vibration coupling, in units of $\sqrt{2}t$). The three PES in each region show, in order of increasing energy, the ground state (g), the OP state (c), and the TP state (e). Region I, stable ground state and bistable OP state; region II, all PES have a single minimum; and region III, the ground-state PES has a double minimum. The TP state always has a single minimum.

($\sqrt{2}t$ units).^{20,23,51,53,54} In the central region (denoted as II), corresponding to systems with intermediate quadrupolar moment ($\rho \sim 0.3-0.6$), all three states have single-minimum PES: dyes belonging to region II have stable nondipolar ground and excited states. In the leftmost region (I), corresponding to systems with low quadrupolar moment ($\rho < \sim 0.2$), the OP state, c, is bistable for sufficiently large ϵ_v values. In this region, the $q_- = 0$ and $\delta = 0$ solution is unstable for the c state, so that symmetry can be broken toward one of two equivalent minima corresponding to states with equal and opposite δ and hence equal and opposite dipole moments. Chromophores belonging to class I have a nondipolar ground state and second excited state (e, the TP state, is undistorted in the whole region of parameters), but the OP allowed state is polar when it localizes in one of the minima. In the third region of the phase diagram (III), corresponding to systems with a large quadrupolar moment ($\rho \rightarrow 1$) and large enough ϵ_v , both the OP and TP states are stable as nonpolar but the ground state is bistable.

The phase diagram in Figure 1 can be rationalized as follows. For $\rho \rightarrow 0$, the ground state corresponds to the almost pure N state and the two excited states correspond to Z_- and Z_+ . In this limit, Z_- and Z_+ are almost degenerate and whatever tiny ϵ_v induces a symmetry breaking in the excited state. In the $\rho \rightarrow 1$ limit, Z_- and Z_+ are lower in energy than N and the ground state almost coincides with Z_+ . The ground state is therefore

almost degenerate with the optically allowed state (Z_-), leading to a charge instability in the ground state itself.

Symmetry breaking in molecular systems (i.e., in finite systems, as opposed to systems such as solids with infinite size) is a complex phenomenon that has been extensively discussed in the literature.^{31,32,55} One of the basic problems is to discriminate between *true symmetry breaking*, where the system is localized in one of the two minima of the PES, and *false symmetry breaking* where, despite having a double-minimum PES, the symmetry is recovered because of the fast switching (tunneling) of the system between the two minima. This is a very interesting fundamental problem; here, we concentrate on the calculation of optical spectra and, to avoid any ambiguity about false symmetry-breaking effects in the adiabatic solution, all spectral properties will be calculated from the direct nonadiabatic solution of the coupled electron-phonon problem.^{26,31,56} Computational details are given in the Experimental Section.

The Hamiltonian in eq 8 describes the low-energy behavior of quadrupolar chromophores in nonpolar solvents. In polar solvents, additional effects are expected related to the coupling of electronic degrees of freedom with the slow orientational motion of polar solvent molecules.^{2,57} In the spirit of the continuum solvation model and adopting exactly the same approach originally developed for dipolar (D- π -A) systems,^{20,23,58} we neglect the minor contributions from quadrupolar and higher order solvation terms and account for the dipolar solvation interaction in the framework of the reaction-field approach. Treating the solvent as an elastic medium, the relevant Hamiltonian reads⁵⁸

$$H_{\text{solv}} = -\mu_0 F_R \hat{\delta} + \frac{\mu_0^2}{4\epsilon_{\text{or}}} F_R^2 \quad (9)$$

where F_R measures the reaction field, whose equilibrium value is proportional to the dipole moment of the solute: $F_R^{(\text{eq})} = (2\epsilon_{\text{or}}/\mu_0^2)\langle \hat{\mu} \rangle$. Here, $\langle \hat{\mu} \rangle$ is the expectation value of the dipole moment operator, $\hat{\mu} = \mu_0 \hat{\delta}$. The parameter ϵ_{or} measures the solvent relaxation energy, i.e., the energy gained by solvent relaxation after the vertical $N \rightarrow Z_{1/2}$ process;^{2,57} ϵ_{or} obviously increases with the solvent polarity. At first sight, eq 9 might suggest that polar solvation is irrelevant for nondipolar chromophores such as the quadrupolar systems discussed in this work. However, when symmetry breaking occurs either in the ground or in the OP state, one ends up with dipolar states and dipolar solvation becomes relevant. More importantly, F_R couples to the same dipolar operator, $\hat{\delta}$, as the q_- coordinate, so that dipolar solvation *cooperates* with vibrational coupling to support symmetry breaking and dipolar distortion. This reasoning based on the physics of operators is in line with standard chemical intuition, suggesting that dipolar states are stabilized in polar environments.

To better understand the role of polar solvation in driving symmetry breaking, Figure 2 shows the PES for the g and c states for a chromophore with $\rho = 0.2$ and $\epsilon_v = 0.2$ (class II). The upper panel refers to a nonpolar solvent ($\epsilon_{\text{or}} = 0$), so that

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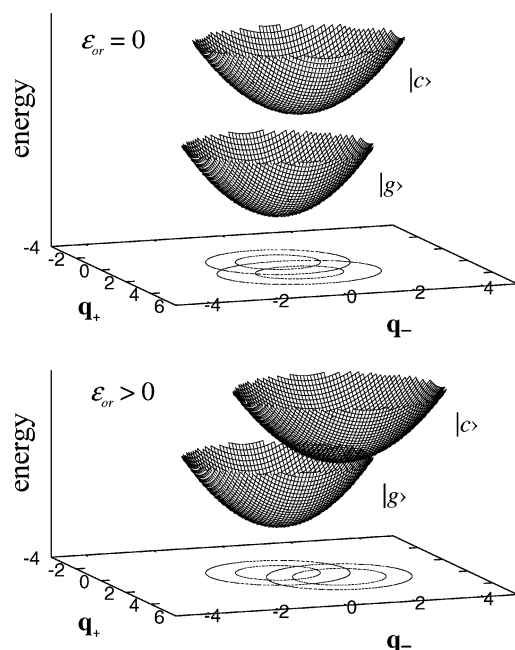


Figure 2. PES for the ground state and the OP-allowed excited state for a chromophore with $\rho = 0.2$, $\sqrt{2}t = 1$ eV, and $\epsilon_v = 0.2$ eV. (Top panel) $\epsilon_{or} = 0$ (apolar solvent); (bottom panel) $\epsilon_{or} = 1$ eV (strongly dipolar solvent) and reaction field (F_R) fixed at its local equilibrium value for the c state.

only the two coordinates q_+ and q_- are relevant. The lower panel refers to a polar solvent ($\epsilon_{or} > 0$), where an additional coordinate, F_R , must be taken into account. For graphical reasons, also in this case, the PES are drawn in the q_+q_- plane, while keeping F_R fixed at its local equilibrium value for the c state [$F_R = (2\epsilon_{or}/\mu_0) \langle c|\hat{\delta}|c\rangle$]: the PES in the lower panel of Figure 2 are then relevant to steady-state fluorescence as occurring from the *relaxed* excited state. Incidentally, the PES relevant to absorption processes (vertical processes starting from the equilibrium ground state) are not affected by the solvent polarity and therefore coincide with the $\epsilon_{or} = 0$ PES in the upper panel. As expected for a class II chromophore, the PES shown in the top panel of Figure 2 ($\epsilon_{or} = 0$) describe stable nonpolar g and c states. Specifically, the PES for the c state has a single minimum, located at $q_- = 0$ (as fixed by inversion symmetry) and finite $q_+ = \sqrt{\epsilon_v} \langle c|\hat{\rho}|c\rangle/\omega$. However, for a large enough ϵ_{or} and for relaxed solvent configuration (i.e., fixing F_R at the equilibrium value for the excited state), the minimum of the excited-state PES moves in the q_+q_- plane, as expected for a state that breaks inversion symmetry (bottom panel of Figure 2). This state with finite q_- is characterized by a finite δ , and hence, the *relaxed* c state has a net dipole moment. Of course, an equivalent minimum exists with opposite dipole moment and opposite F_R . Therefore, as far as symmetry breaking is concerned, the *total relaxation energy* (vibrational plus solvation contributions) is the key quantity: only when a threshold value for the total relaxation energy is reached does symmetry breaking occur. This implies that, for systems with a small ϵ_v , symmetry can be broken only for large ϵ_{or} and thus a marked fluorescence solvatochromism will be observed only in highly polar solvents.

For example, the system considered in Figure 2 breaks symmetry in the excited state only for $\epsilon_{or} > 0.5$. The value of ϵ_{or} for a given solvent strongly depends upon the dimension and shape of the solute molecule, being on the order of 0.5–

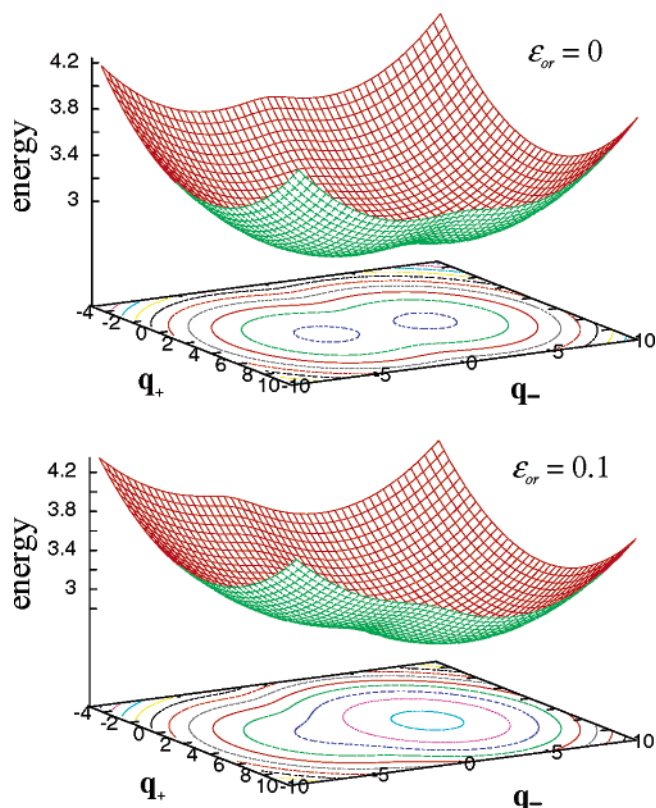


Figure 3. PES for the OP-allowed excited state for a class I chromophore with $\rho = 0.07$, $\sqrt{2}t = 0.6$ eV, and $\epsilon_v = 0.3$ eV. (Top panel) $\epsilon_{or} = 0$ (apolar solvent); (bottom panel) $\epsilon_{or} = 0.1$ eV (low–medium polarity solvent) and reaction field (F_R) fixed at its local equilibrium value for the c state.

1.0 eV for highly dipolar solvents [such as dimethyl sulfoxide (DMSO)] and for a solute cavity relevant to typical push–pull chromophores (radius on the order of 5 Å).^{20,23,54,58,59} For elongated molecules, such as typical quadrupolar (D- π -A- π -D or A- π -D- π -A) chromophores, the shape of the cavity is hardly approximated by a sphere, so that precise estimates are difficult. In any case, our model does not rely on any specific microscopic model for ϵ_{or} but extracts its value from experimental data. We underline that not all systems belonging to class II undergo symmetry breaking as a result of polar solvation: for intermediate values of ρ (approximately $0.25 < \rho < 0.6$), symmetry breaking is not expected, at least for realistic ϵ_{or} values.

A different case is shown in Figure 3 where we plot the PES relevant to state c for a chromophore with $\rho \approx 0.1$ and a large enough electron–vibration coupling ($\epsilon_v = 0.5$ units of $\sqrt{2}t$) as to lead to a double-minimum PES (class I) already in nonpolar solvents (top panel, $\epsilon_{or} = 0$). In this case, already in slightly polar solvents (bottom panel, small ϵ_{or}), a sizable stabilization of the polar broken-symmetry state is expected: important fluorescence solvatochromism is thus predicted already in weakly polar solvents. Of course, an equivalent “mirror image” minimum as the one described in the bottom panel of Figure 3 develops at opposite q_- and F_R values.

It is important to realize that the *vertical* excited-state always maintains the symmetry of the ground state, so that for chromophores having a centrosymmetric ground state (class I and II) absorption frequencies are basically unaffected by polar solvation (only inhomogeneous broadening effects are expected

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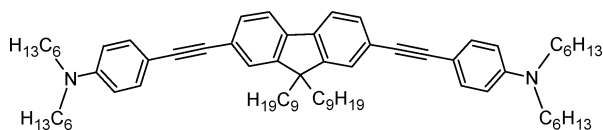


Figure 4. Molecular structure of compound **1**.

in absorption bands, as discussed in the analysis of chromophore **1**). On the opposite, steady-state fluorescence occurs from the relaxed c state, which, for class I chromophores, is polar (at least in polar solvents): large positive fluorescence solvatochromism is thus expected. PES in Figure 3 also help to underline the different roles played by vibrational and solvation degrees of freedom with respect to symmetry breaking. As discussed above, both polar solvation and vibrational coupling have similar effects (and indeed cooperate) in favoring the appearance of double-minima (bistable) PES. However, solvation and vibrational motions have very different time scales: vibrational coordinates (typically in the mid-infrared region) describe a truly quantum mechanical motion, so that, depending upon the height of the barrier between the two minima, a fast interconversion (tunneling) between the two broken-symmetry states may restore the original symmetry (the false symmetry-breaking case).⁵⁵ Instead, polar solvation can be described in terms of a very slow (actually overdamped) coordinate that behaves as a classical coordinate⁶⁰ and therefore does not support tunneling. In other words, interconversion between the two equivalent broken-symmetry minima is extremely slow in polar solvents because it requires the motion along a slow classical coordinate. Of course, both minima (i.e., both solute–solvent conformations) are equally probable and hence are equally populated: relevant spectra are however exactly the same and simply sum up in spectra calculated as Boltzmann averages over solvation coordinates^{20,23} (see also Calculation Details in the Experimental Section).

Symmetry Breaking in Action: Fluorescence Solvatochromism

As already anticipated, several examples are reported in the literature of quadrupolar chromophores exhibiting strongly solvatochromic fluorescence.^{10,13,18,36,48} In these systems, a benzenoid structure typically corresponds to the N resonating form. The quinoidal structures associated with either Z_1 or Z_2 have therefore a much higher energy ($2\eta \gg 0$), and their contribution to the ground state is small: these chromophores have small quadrupolar moments (approximately $\rho < 0.2$) and belong to class I. In this section, we will discuss in detail linear absorption and fluorescence spectra as well as TPA spectra for two specific chromophores of this kind, to assess and clearly identify the spectroscopic effects of bistability and symmetry breaking.

Example 1. The first example is a newly synthesized chromophore (**1**), sketched in Figure 4, characterized by two external electron-donor amino groups and a central fluorene core acting as an electron-acceptor moiety.^{12,61}

Photophysical properties of chromophore **1** dissolved in solvents of increasing polarity are summarized in Table 1; experimental absorption and fluorescence spectra are shown in

Table 1. Solvation Effects on Photophysical Properties of **1**

solvent	λ_{abs} (nm)	λ_{em} (nm)	Stokes shift (cm^{-1})	dielectric constant ^a	τ^b (ns)	Φ^c	τ_0^d (ns)
toluene	387	421	2100	2.4	0.74	0.80	0.93
CHCl_3	389	433	2600	4.8	0.80	0.86	0.93
hexanol	385	450	3600	13.3	0.93	0.83	1.12
acetone	387	482	5100	20.7	1.42	0.83	1.72
CH_3CN	388	503	5900	37.5	1.67	0.96	1.75

^a Solvent dielectric constant at 20 °C. ^b Measured fluorescence lifetime. ^c Fluorescence quantum yield. ^d Radiative lifetime derived as $\tau_0 = \tau/\Phi$.

Figure 5a; and Figure 5b shows the TPA spectrum collected in toluene. Molecule **1** shows a marked fluorescence solvatochromism, while the absorption spectrum is almost independent of the solvent polarity. The TPA spectrum presents a weak shoulder in correspondence with the transition toward the OP allowed state and a second strong transition corresponding to the e state, whose maximum is located beyond the experimentally accessible spectral region.

These data can be used to test the proposed model and shed light on the photophysical behavior of the chromophore. Molecular model parameters can be readily estimated from spectroscopic data in the nonpolar solvent (toluene). The frequencies of the maximum of the linear absorption and TPA (ω_{gc} and ω_{ge} , respectively) fix ρ and $\sqrt{2}t$ (and hence η , see eq 4).

The TPA maximum is not experimentally accessible, but we locate it between 700 and 720 nm (transition wavelength between 350 and 360 nm) by comparison with data on related chromophores.^{8,11,62,63} The molecular parameters describing vibrational coupling, ω_v and ϵ_v , are fixed as to reproduce the Frank–Condon progression in the absorption (or fluorescence) spectrum. Finally, the bandwidth (half-width at half-maximum, HWHM) associated to each transition is estimated from experimental spectra, and μ_0 is fixed to correctly reproduce the measured extinction coefficient. This procedure allows us to calculate the spectra reported in parts c and d of Figure 5, relevant to toluene (black lines). Spectra in other solvents are obtained by introducing the solvation term in our Hamiltonian and tuning the *single* parameter ϵ_{or} that accounts for solvent polarity, while *all of the molecular parameters are kept fixed, independent of the solvent*. Colored lines in Figure 5c show spectra calculated for the ϵ_{or} values in the legend. Calculated spectra reproduce main experimental features. Specifically, the frequency of the absorption band is barely affected by the solvent polarity. The main effect of polar solvation is recognized in the inhomogeneous broadening of the absorption band: in agreement with experimental data, the vibronic structure, resolved in low-polarity solvents, is progressively smeared out with increasing solvent polarity. We underline that the calculated broadening is a genuine result of our solvation model: the HWHM for the vibronic lines is in fact exactly the same for all calculated spectra. The strong solvatochromism observed in steady-state fluorescence is well-reproduced by our model.

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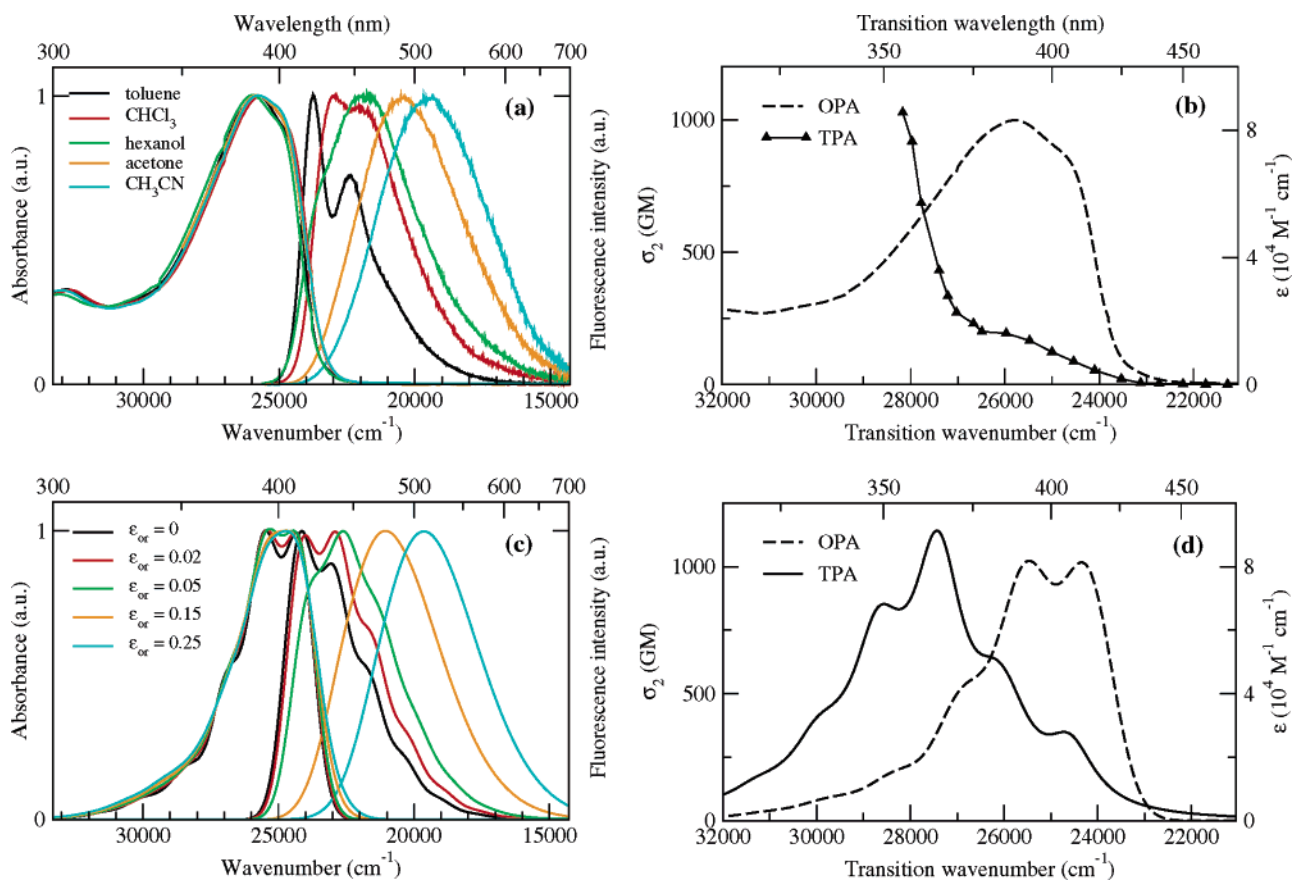


Figure 5. Spectra of compound **1**. (Left panels) Experimental (a) and calculated (c) absorption and fluorescence spectra in solvents of increasing polarity. (Right panels) Experimental (b) and calculated (d) OPA and TPA spectra of **1** in toluene. 1 GM = 10⁻⁵⁰ cm⁴ s photon⁻¹. Calculated spectra have been obtained by fixing the following parameters: $\eta = 1.50$ eV, $\sqrt{2t} = 0.60$ eV, $\omega_v = 0.16$ eV, $\epsilon_v = 0.30$ eV, HWHM = 0.08 eV, and $\mu_0 = 40$ D. Values for ϵ_{or} are in the legend (in electronvolts).

Moreover, calculated spectra also reproduce the evolution of the emission band shape with the solvent polarity: in particular, the evolution of the Frank–Condon profile is described by our results, with a progressive borrowing of intensity of the 0– n vibronic transitions at the expense of the 0–0 line. Again, this is a genuine result: ϵ_v is kept constant in all solvents. Whereas the model well-reproduces the observed trends, small discrepancies are observed. The Stokes shift calculated in the less polar solvent (toluene) is underestimated: this could be cured by assigning toluene a small ϵ_{or} value, as suggested by empirical polarity scales.^{2,64} Conformational or torsional degrees of freedom represent another source of the Stokes shift in nonpolar solvents and may also cure the minor discrepancy between calculated and experimental line shapes in toluene.^{20,65}

On the basis of the analysis of spectroscopic data, chromophore **1** can be classified as a low-quadrupolar molecule ($\rho \approx 0.07$) and the relevant $\epsilon_v = 0.5$ (units of $\sqrt{2t}$) clearly locates it in the I region of the phase diagram, where the c state PES have a double minimum even in nonpolar solvents. Indeed, the PES in Figure 3 are obtained for parameters relevant to **1**. The appearance of a double-minimum c state PES already in nonpolar solvents naturally explains the lack of mirror-image symmetry between absorption and fluorescence spectra measured in toluene. In fact, in the case of a double-minimum

excited-state PES, the Franck–Condon factors can be significantly different for the absorption and fluorescence processes: the absorption process occurs from the lowest vibrational eigenstates of the single-minimum ground state toward the unrelaxed (Franck–Condon) eigenstates of the double-minimum excited-state PES, while the fluorescence process stems from the lowest vibrational eigenstate of the double-minimum excited-state PES to the (Franck–Condon) eigenstates of the single-minimum ground state. The strong dependence of fluorescence spectra on the solvent polarity, even for solvents with very low polarity (cf. spectra in toluene and chloroform in Figure 5), is also linked to the double-minimum nature of the excited state. In fact, upon vertical absorption, the system reaches a bistable state, so that even a very weak perturbation as a result of the interaction with a slightly dipolar solvent breaks the molecular symmetry and creates a polar excited state, stabilized in polar solvents. The evolution of the fluorescence frequency with the solvent polarity can be approximated as $\hbar\omega_{cg} = \hbar\omega_{cg}^{(0)} - \mu_{cc}\Delta f/r^3$, where r is the cavity radius and $\Delta f = (\epsilon - 1)/(2\epsilon + 1) - (n^2 - 1)/(2n^2 + 1)$ is the solvent polarity indicator (ϵ and n are the solvent dielectric constant and refractive index, respectively).⁶⁶ If μ_{cc} was independent of the solvent polarity, a straight line would be obtained for ω_{cg} versus Δf . Instead, data in Figure 6a sharply deviate from linearity, suggesting a large variation

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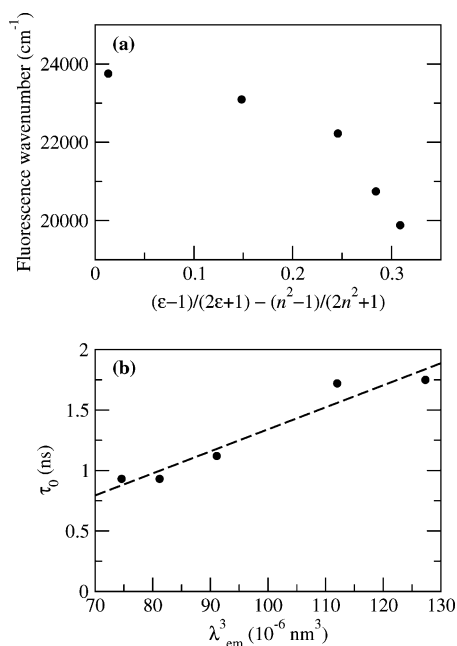


Figure 6. (a) Emission frequency of compound **1** versus the solvent polarity indicator (ϵ is the dielectric constant, and n is the refractive index). (b) Radiative lifetime versus λ_{em}^3 (●) and corresponding linear regression (---).

of the dipole moment of the relaxed excited state with the solvent polarity.

On the basis of the analysis of linear spectra of chromophore **1**, we estimate the dipole moment for the relaxed excited state as $\mu_{cc} = 0, 20, 33, 36,$ and 37 D in toluene, CHCl_3 , hexanol, acetone, and CH_3CN , respectively. The relaxed excited state is nonpolar in toluene (a case of false symmetry breaking) and acquires an increasing dipolar character (real symmetry breaking) with increasing solvent polarity, reaching an almost “saturated” value in hexanol, in qualitative agreement with data in Figure 6a. While a strong evolution of the dipole moment in the relaxed excited state is predicted and observed, only a $\sim 20\%$ variation of the squared transition dipole moment for the fluorescence process is calculated when going from apolar to highly polar solvents. If we consider the well-known relation $1/\tau_0 \propto \mu_{trans}^2 \omega_{trans}^3$,⁶⁷ we can easily verify that the solvent dependence of τ_0 can indeed be mainly ascribed to the solvent dependence of the fluorescence frequency (see Figure 6b) in agreement with calculated results.

TPA spectra also deserve some comments. The calculated TPA spectrum reported in Figure 5d compares favorably with experimental data (Figure 5b), even if a complete comparison is hindered by experimental limitations.⁶⁸ In the available spectral region, both the absolute value of the TPA cross-section and the TPA band shape are well-reproduced. The TP e state never undergoes symmetry breaking (see Figure 1). However, the coupling between electronic degrees of freedom and the antisymmetric vibrational coordinate (q_-) has interesting consequences on TPA spectra. In fact, the shoulder observed in the TPA spectrum in correspondence with the OP allowed state is quantitatively reproduced in our model and can be assigned

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(68) The calculated position for the TPA band is probably slightly red-shifted with respect to what can be experimentally estimated, but this goes with the parallel shift of the OPA band (see the previously discussed Stokes-shift problem).

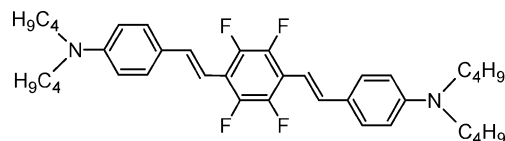


Figure 7. Molecular structure of compound **2**.

to the vibronic activation of the otherwise TP forbidden c state. Specifically, the two low-energy shoulders in the calculated TPA spectrum are assigned to a vibronic activation of the c state as a result of the coupling with antisymmetric q_- vibrations, while the successive more intense peaks correspond to genuine $g \rightarrow e$ transitions, with the 0–0 line being the strongest one. Our results, rule out alternative explanations based on the deviation of the molecular structure from linearity.

Example 2. As a second example, we discuss results from ref 13 relevant to the centrosymmetric D- π -A- π -D molecule **2**, sketched in Figure 7.

Similar to chromophore **1**, a strong solvatochromism is observed in fluorescence, whereas no dependence of the absorption band on the solvent polarity is reported. Interestingly, solvatochromic studies of the dipolar D- π -A analogue show that the fluorescence solvatochromism of quadrupolar compound **2** is of the same order of magnitude as that for the dipolar counterpart. In ref 13, this strong fluorescence solvatochromism was ascribed to solute quadrupole–solvent dipole interactions, following a formulation from Suppan.⁶⁹ This formalism is however flawed: by symmetry reasons, a quadrupolar charge distribution cannot induce a *uniform* reaction field at the location of the solute. Of course, field gradients can occur at the solute location, but these cannot be described by introducing a single solvation coordinate (i.e., a uniform electric field). On physical grounds, these quadrupolar (or higher multipolar) contributions to solvation are expected to be much smaller than dipolar ones. We therefore suggest that the observed behavior is again due to symmetry breaking in the relaxed excited-state because of polar solvation. Following the same procedure already described for **1**, we estimate model parameters for chromophore **2**. The calculated absorption, fluorescence, and TPA spectra are reported in Figure 8, where black lines are relevant to the nondipolar solvent, whereas colored lines refer to solvents of increasing polarity. These spectra are in good agreement with those reported in ref 13; not only are transition energies and hence fluorescence solvatochromism well-reproduced, but also band shapes and absolute intensities of linear absorption and TPA compare favorably with experimental data.

For **2**, we estimate $\rho \approx 0.13$, i.e., a quadrupolar character that is almost twice that of **1**. Accordingly, we expect a less pronounced instability for the c state. Indeed, for the adopted model parameters, the PES relevant to the OP state presents a double minimum but with a very low barrier (about half a vibrational quantum). This is the reason why absorption and fluorescence spectra in the nonpolar solvent have very similar vibronic progressions (at variance with chromophore **1**, for which the barrier amounts to about two vibrational quanta). Again, the dipole moment calculated for the relaxed excited-state of **2** vanishes in the nonpolar solvent, to attain a sizable

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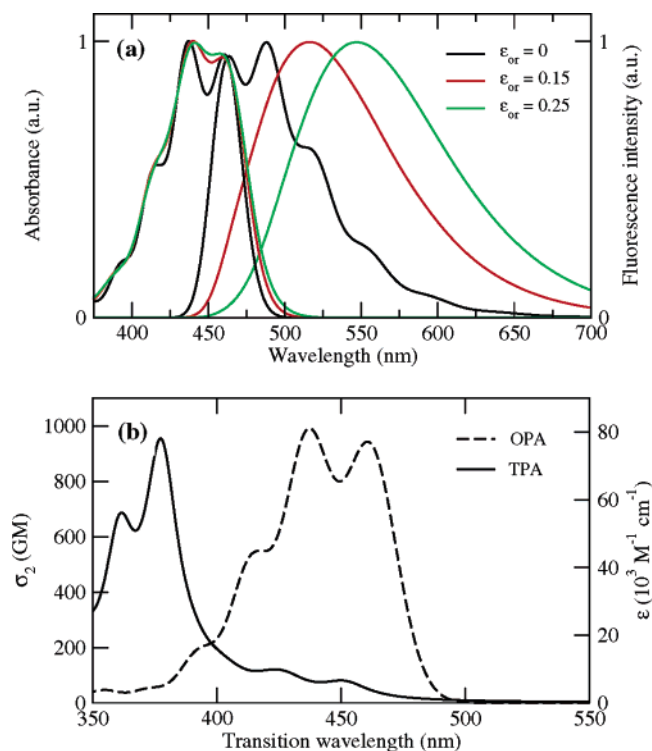


Figure 8. Calculated spectra for compound **2**. (a) Absorption and fluorescence in solvents of increasing polarity; (b) OPA and TPA in an apolar solvent. Calculated spectra have been obtained by fixing the following parameters: $\eta = 1.25$ eV, $\sqrt{2}t = 0.80$ eV, $\omega_v = 0.15$ eV, $\epsilon_v = 0.42$ eV, HWHM = 0.07 eV, and $\mu_0 = 28$ D. Values for ϵ_{or} are in the legend (in electronvolts).

value in THF (21 D) and CH_3CN (22 D). The calculated TPA spectrum presents two weak shoulders in correspondence to the transition toward the OP allowed state (see Figure 8b): this phenomenon is again due to a weak vibronic activation of the c state. The experimental spectrum does not allow us to conclude if this feature is actually present. In any case, these vibronic bands in the TPA spectrum are calculated much less intense than for **1**, a phenomenon that is again due to the stronger quadrupolar character of **2**.

Highly Quadrupolar, Symmetry-Preserving Systems

Squaraine-based quadrupolar dyes show minor solvatochromism both in absorption and fluorescence.⁷⁰ For these chromophores, only one study of TPA is available in the literature, reporting data collected with nanosecond excitation pulses.³⁵ To obtain more reliable data, we have synthesized a squaraine dye (**3** in Figure 9). Absorption and fluorescence spectra of **3** have been collected in several solvents, and its TPA spectra have been measured using femtosecond pumping, to minimize spurious contributions.

Photophysical properties of **3** are summarized in Table 2. Absorption and fluorescence spectra as well as the TPA profiles of **3** in solvents of different polarity are shown in parts a and b

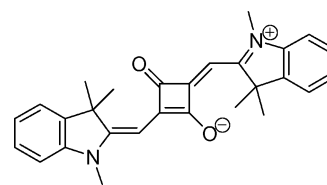


Figure 9. Molecular structure of compound **3**.

Table 2. Photophysical Properties of **3** in Solvents of Different Polarity

solvent	dielectric constant	refractive index	λ_{abs} (nm)	λ_{em} (nm)	Stokes shift (cm^{-1})	ϵ^a ($\text{cm}^{-1} \text{M}^{-1}$)	Φ
toluene	2.38	1.497	639	648	215	330 000	0.66
CHCl_3	4.81	1.446	633	642	235	305 000	0.43
DMSO	46.7	1.478	641	652	265	280 000	0.20

^a Molar extinction coefficient.

of Figure 10, respectively. Linear spectra confirm that chromophore **3** is only marginally solvatochromic, both in absorption and in emission (10 nm excursion in a wide range of solvent polarities). As for TPA spectra in CHCl_3 , we confirm results in ref 35, with a maximum at 820 nm, even if the actual cross-section is about 40% lower than reported in ref 35 (in which TPA measurements were conducted using nanosecond pumping). Measurements in other solvents however suggest that the peak at 820 nm does not correspond to the maximum of the TPA band but that the TPA signal increases further in the region below 800 nm that, quite unfortunately, is not accessible with our experimental setup. Indeed, results reported in ref 13 for two squaraine-based dyes (there labeled **13a** and **13e**) having similar structures indicate cross-sections differing by an order of magnitude: this discrepancy can be understood in the light of our data, suggesting that the band at 820 nm is just a shoulder of a probably much more intense TP transition placed below 800 nm. While this is quite clear from our measurements in toluene and DMSO solutions, the increase of σ_2 with respect to the 820 nm maximum is not detected for the CHCl_3 solution when moving down to 800 nm (Figure 10b). The different behavior in CHCl_3 with respect to toluene and DMSO can be ascribed to a small blue shift of the band (see linear absorption spectra) or to possible photodegradation problems [as suggested by the fact that the dependence of the two-photon-excited fluorescence (TPEF) response on the incident intensity is quadratic only for low intensities in that particular solvent].

In any case, fixing the TPA frequency between 800 and 700 nm and making use of linear absorption data, we obtain a crude estimate of the model parameters. Specifically, we estimate $\rho \approx 0.4$ and $\epsilon_v \approx 0.13$ (units of $\sqrt{2}t$), so that squaraine **3** can be located in region II of the phase diagram in Figure 1, suggesting that for this chromophore all states of interest for spectroscopy maintain a nondipolar character. In these conditions, solvation effects are not able to break the symmetry of the system. This explains why no noticeable solvatochromism is observed either in absorption or in fluorescence spectra. The observation of a residual weak solvatochromism can be attributed to the difference in the solvent refractive indexes (see Table 2). Moreover, at variance with chromophores of class I, inhomogeneous broadening is not effective in absorption nor in emission spectra. This confirms the large quadrupolar character of **3**, because for dyes with large ρ (approximately $\rho > 0.2$), the dependence of

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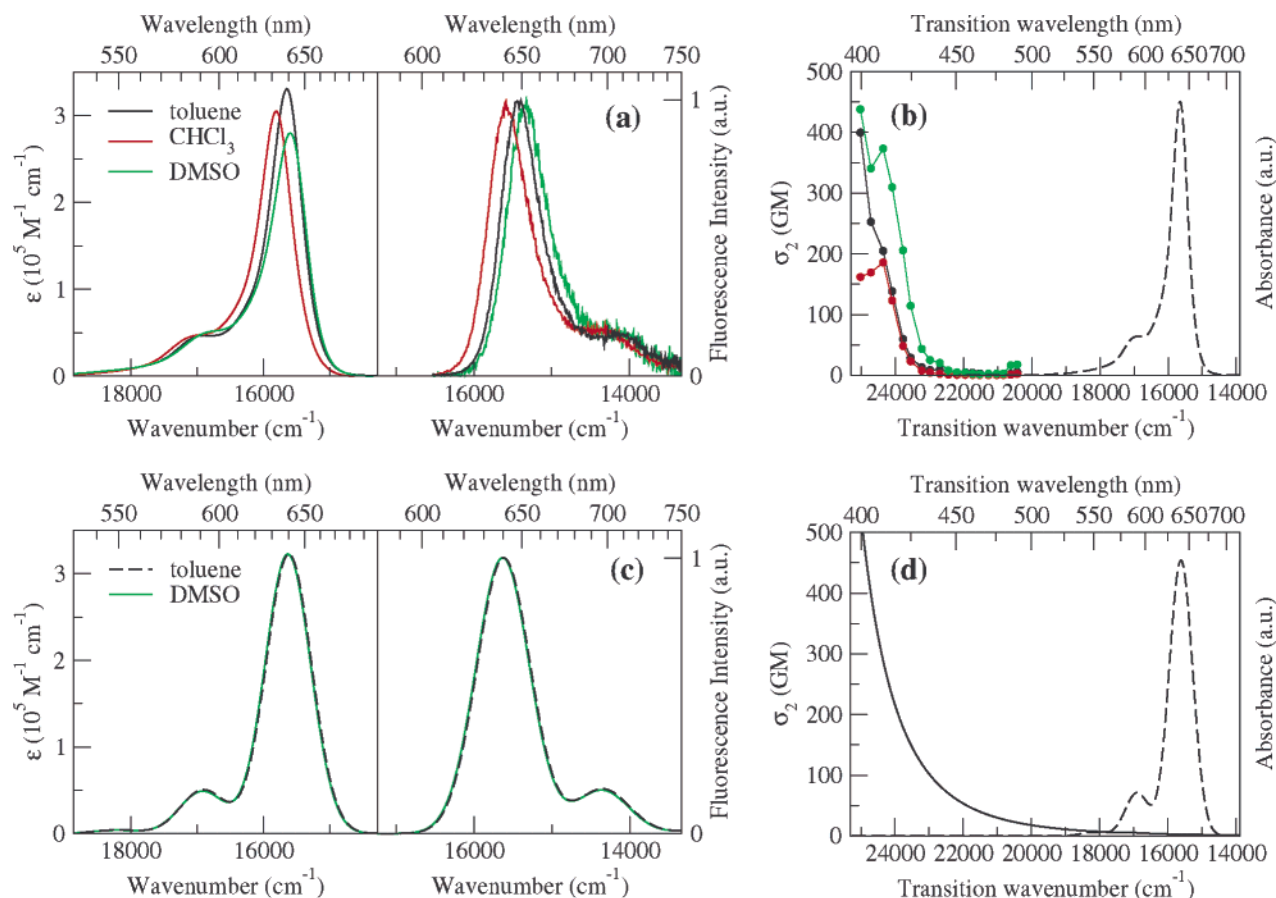


Figure 10. Spectra of compound 3. (Top panels) Experimental absorption and fluorescence (a) and TPA spectra (b) in solvents of increasing polarity (the OPA spectrum in toluene is reported for a comparison). (Bottom panels) Calculated absorption and fluorescence in two solvents of different polarity (c) and TPA spectrum in an apolar solvent (d) (the OPA spectrum is reported for a comparison). Calculated spectra have been obtained by fixing the following parameters: $\eta = 0.28$ eV, $\sqrt{2}t = 1.20$ eV, $\omega_v = 0.16$ eV, $\epsilon_v = 0.16$ eV, HWHM = 0.05 eV, and $\mu_0 = 21$ D. $\epsilon_{or} = 0$ and 0.25 eV for toluene and DMSO, respectively.

the transition frequency on ρ is smooth, leading to negligible inhomogeneous broadening effects.

The same analysis can be extended to chromophore **13e** in ref 35, for which we estimate $\rho \approx 0.3$, with a TPA cross-section on the order of 9000 GM, in reasonable agreement with the reported one. This squaraine dye is then also placed in region II of the phase diagram in Figure 1, with no symmetry-breaking phenomena in either the ground or excited state.

Discussion and Conclusions

This paper presents a joint theoretical and experimental work aimed to understand the interesting and variegated spectroscopic behavior of quadrupolar dyes, an interesting family of molecules for NLO applications. These chromophores represent typical examples of molecules where the coupling between electronic and vibrational degrees of freedom play a significant role in governing their optical responses (in the ground and/or excited states). The coupling between electronic and vibrational degrees of freedom indeed governs structural instabilities in a variety of extended systems with delocalized electrons and/or extended charge resonance, including polymers, charge-transfer salts, and mixed-valence chains.⁷¹ Instabilities

in finite *molecular* systems are also an active research field,^{32,40,72,73} where, however, the subtle distinction between static and dynamic effects makes the problem much more complex than in extended systems.^{32,55} Here, we focus on the spectroscopic consequences of broken-symmetry states in quadrupolar organic dyes for NLO applications. On the basis of a few-state description of the charge-transfer processes that characterize the low-energy physics of these systems and accounting for the coupling between electrons and slow degrees of freedom, including molecular vibrations and effective polar solvation coordinates, we propose a general reference frame to understand the spectroscopic behavior of quadrupolar molecules in solution.

For molecules with a low quadrupolar moment, both the ground and TPA states are stable. The OP allowed state is instead conditionally unstable: for a large enough coupling to molecular vibrations, the relevant PES show two minima corresponding to the two equivalent broken-symmetry structures with polar nature (class I). In this case, after vertical excitation, the system relaxes toward one of the two minima, leading to a polar relaxed excited state. Polar states are stabilized in polar solvents: symmetry breaking may appear as a result of the combined action of vibrational and solvation coupling in systems

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where vibrational coupling by itself would lead to stable OP allowed states. The polar nature of the relaxed OP state is responsible for the positive solvatochromic behavior of steady-state fluorescence observed for this class of dyes, in sharp contrast with the nonsolvatochromic absorption spectra.

In dyes with intermediate quadrupolar character (class II), the large mixing between neutral and charge-separated states guarantees a sizable energy splitting between all relevant states and hence a good stability of the system. Because all states maintain their nonpolar character, no major solvatochromic effects are expected for this class of dyes, represented, e.g., by squaraine-based dyes. For large quadrupolar dyes (class III), instead, the OP state is very low in energy and the ground state becomes conditionally unstable. Large inverse solvatochromic behavior is then predicted for these dyes in absorption, whereas fluorescence spectra, occurring from a nonpolar state, should be unaffected by the solvent polarity.

Many experimental data have been collected for dyes of class I: here, we discussed a few specific examples. For these dyes, we quantitatively account for the large positive solvatochromism observed for steady-state fluorescence spectra and solvent-independent absorption frequency. More subtle effects, including the lack of mirror-image symmetry between absorption and fluorescence bands, the inhomogeneous broadening of absorption bands in polar solvents, as well as the appearance of vibronically activated TPA features in the region of OP states, are naturally understood in the proposed picture. Quantitative agreement with the TPA cross-section further validates the picture.

In contrast to chromophores belonging to class I, data on chromophores belonging to class II are scanty. Our work suggests that squaraine-based dyes belong to this class of molecules. Indeed, no major solvatochromism is observed for squaraines neither in absorption nor in fluorescence.⁷⁰ Large TPA cross-sections are expected for dyes with intermediate quadrupolar character, but care has to be taken, because as $\rho \rightarrow 0.5$, we expect TPA absorption to occur just at twice the energy of the OPA: one-color TPA spectra would then be masked by the OPA signal. To the best of our knowledge, no example of chromophores belonging to class III is known: we hope that this work will trigger synthetic effort in this direction. Cyanine-based dyes, with typical absorption in the near-infrared region, usually bear a positive charge, so that the present model is not directly applicable. It is however interesting to notice that for some of these dyes evidence of symmetry breaking in the ground state has been reported in polar solvents.⁷⁴

Solvent-induced symmetry breaking has been recently proposed for the ground state of I_3^- .⁷² Whereas this phenomenon is superficially equivalent to our result for chromophores of class III, we underline that for I_3^- specific solute–solvent interactions (such as, e.g., hydrogen bonds) are considered to be responsible for the phenomenon, while we predict ground- (or excited-) state symmetry breaking in a continuum model for solvation, where any site-specific interaction is ruled out. Symmetry breaking in the ground state has been extensively discussed as a consequence of electron–phonon coupling in mixed-valence binuclear metal-

lic complexes.^{31,32,55} Indeed, relevant models have some common features with our model, with the main difference being related to the different nature of the electronic Hamiltonian.

Symmetry breaking (localization) in the excited state is an actively investigated topic in recent years.^{18,38,43,44,47,49,75} Specifically, the excited-state symmetry breaking predicted by our model for chromophores of class I is in line with recent results reported in ref 18, where time-dependent density-functional theory (TD-DFT) calculations predict the appearance of broken-symmetry solutions for the relaxed excited-state of quadrupolar and octupolar chromophores. Our work generalizes these results for quadrupolar dyes, to account for solvation effects and their consequences in linear and nonlinear spectra. Very recently, the occurrence of symmetry breaking in the excited state of a family of donor–acceptor–donor π molecules has been discussed on the basis of a phenomenological model.³⁶ Our microscopic model is based on an essential-state description of the electronic system that represents the reference model for quadrupolar chromophores^{50,51} and can be easily extended to multipolar chromophores. The role of vibrations and solvation coordinates is discriminated, a particularly important issue in view of their different time scales and their different roles in distinguishing between true and false symmetry breaking. In this context, the use of nonadiabatic techniques is instrumental.

The essential-state model adopted here to describe the basic physics of quadrupolar chromophores leads to a *general* phase diagram for this class of molecules, describing symmetry-breaking phenomena in either the OP excited-state or the ground state, as well as cases where symmetry breaking is not supported, neither by electron–vibration coupling nor by solvation interactions. The phase diagram in Figure 1 can in fact be used to guide the design of chromophores with specific photophysical behavior. For example, if a solvatochromic fluorescence is sought (e.g., for sensing of micropolarity), quite neutral chromophores with sizable electron–phonon coupling should be synthesized; on the contrary, if solvatochromism is not desirable (e.g., when insensitiveness to the environment is sought), more quadrupolar chromophores should be designed, quite independently of their electron–phonon coupling. At the same time, on the basis of their solvatochromic behavior, quadrupolar dyes can be easily assigned to one of the three classes in the phase diagram in Figure 1, so that important information can be obtained on their quadrupolar character (ρ). The value of ρ allows us to estimate the TPA cross-section, as known by the three-state electronic model.⁵⁰ Therefore, the proposed model, via easily accessible experimental data (OPA and fluorescence), can give important clues on the TPA efficiency of quadrupolar dyes, thus helping the design and the first selection of quadrupolar molecules with optimized properties. For example, chromophores showing no absorption solvatochromism and strong fluorescence solvatochromism already appreciable in slightly polar solvents belong to class I and are expected to have comparatively small TPA cross-sections. Quadrupolar chromophores showing appreciable fluorescence solvatochromism only in highly polar solvents can instead be located in region II of the phase diagram but close to region I (see example in Figure 2): these dyes have higher TPA cross-sections with respect to dyes in region I. The best TPA cross-sections are expected for

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chromophores being nonsolvatochromic at all, i.e., well within region II (intermediate quadrupolar character, such as, e.g., squaraine dyes). However, in this last case, care has to be taken, because as $\rho \rightarrow 0.5$, the very intense TP absorption overlaps with the OPA signal, thus suppressing many of the specific features of TPA (such as 3D resolution and linear transparency).

The symmetry-breaking phenomenon occurring in the c state as a result of electron-vibration coupling and/or polar solvation is clearly associated with the localization of the excitation in one of the two arms of the chromophore. The problem of localization/delocalization of excitations is a major issue in the study of branched structures, starting from quadrupolar or octupolar chromophores up to all-conjugated dendrimers.^{43,45} Understanding the energy-transfer processes in such molecules is extremely important with respect to many potential applications. Besides NLO applications, multipolar systems are currently studied as model systems for the mechanism of energy redistribution and the dynamics of electronic coupling in dendritic structures,⁴³ two basic concepts for controlling the energy flux to design and obtain artificial light/energy-harvesting systems.^{43,76}

The work we presented touches upon several fundamental issues, ranging from vibrationally and/or solvent-induced symmetry breaking, to excitation localization/delocalization phenomena, to solvent and vibronic effects in linear and nonlinear optical spectra. The proposed model sets the basis toward understanding the physics of a class of molecules of interest for advanced applications and can be quite easily extended to more complex structures (e.g., octupoles and dendrons): this shall offer a basis to develop reliable guidelines for the synthesis of chromophores and chromophore-based nanoscale systems with optimized properties.

Experimental Section

Synthesis. The synthesis of the bis-donor quadrupole **1** is based on a one-pot double Pd^{II}-catalyzed cross-coupling reaction of the fluorene-colored building block 2,7-diethynyl-9,9-dinonyl-9H-fluorene with the iodide derivative *N,N*-dihexyl-4-iodobenzenamine as described in ref 77. The squaraine dye **3** was synthesized from squaric acid and corresponding methylene base, using similar experimental conditions as reported in ref 35.

Photophysical Methods. UV/vis spectra were recorded on a Jasco V-570 spectrophotometer. Fluorescence spectra were obtained at room temperature in dilute solutions ($\sim 10^{-6}$ M, taking care that the optical density was less than 0.1, to minimize internal absorption) using an Edinburgh Instruments (FLS 920) spectrometer in photon-counting mode. Emission spectra of compound **1** have been obtained by exciting at the maximum absorption wavelength in each solvent. The excitation wavelength was set to 600 nm for compound **3**. Fluorescein in 0.1 N NaOH was used as a standard (quantum yield $\Phi = 0.90$)⁷⁸ for determining fluorescence quantum yields.

TPA cross-sections (σ_2) were determined by the TPEF technique in solution (concentration between 10^{-5} and 10^{-4} M). These measurements provide the TPEF action cross-section $\sigma_2\Phi$. The corresponding σ_2 values were derived by determining the fluorescence quantum yield Φ from standard fluorescence measurements. TPEF measurements were conducted using a mode-locked Ti:sapphire laser operating between 700 and 1000 nm and delivering 120 fs pulses at 76 MHz, following the

experimental protocol described in detail by Xu and Webb.⁷⁹ Emission was detected in epifluorescence mode, avoiding inner-filter effects related to the high dye concentrations by focusing the laser near the cuvette window. Quadratic dependence of the fluorescence intensity on the excitation intensity was verified for each data point. TPEF measurements were calibrated relative to the absolute TPEF action cross-section determined by Xu and Webb for fluorescein in water (pH 11) in the 690–1000 nm range.⁷⁹ Equations for relative determination of σ_2 were adopted as reported in ref 80. Experimental uncertainty does not exceed $\pm 10\%$.

Calculation Details. The Hamiltonian in eq 8 can be numerically diagonalized on the basis obtained by the direct product of the three electronic basis states, $|N\rangle$, $|Z_1\rangle$, and $|Z_2\rangle$, and of the reference vibrational states, i.e., the eigenstates of the harmonic oscillators in the last two terms of eq 8. The basis is truncated by fixing a maximum number of phonon states, M ; the corresponding $3M \times 3M$ matrix can be diagonalized up to fairly large M values, yielding numerically exact nonadiabatic eigenstates. The minimum M required to get convergence depends upon the model parameters and the properties of interest. All results presented in this work have been obtained with $M = 10$.

Linear absorption and fluorescence spectra are calculated by assigning each transition a Gaussian line shape with HWHM. In polar solvents, thermal disorder in the solvation coordinate locally affects the solute properties, so that the solution can be described in terms of a Boltzmann distribution of solute molecules with different ρ , each one in equilibrium with the local configuration of the surrounding solvent. Absorption and emission spectra in polar solvents are then obtained by summing up the spectra calculated for molecules with different ρ , weighted by their Boltzmann probability.²⁰

The TPA cross-section is calculated according to the following expression (cgs units):^{9,81}

$$\sigma_2(\omega) = \frac{4\pi^2\hbar\omega^2}{c^2n^2} \text{Im}\langle\gamma(-\omega;\omega,\omega,-\omega)\rangle \quad (10)$$

where c is the speed of light, n is the solvent refractive index, and $\langle\gamma\rangle$ is the orientationally averaged second hyperpolarizability. This expression is consistent with an expansion of the polarization in a Taylor series with respect to the total electric field⁸²

$$p = p_0 + \alpha E + \frac{1}{2!}\beta E E + \frac{1}{3!}\gamma E E E + \dots \quad (11)$$

Tensor elements of $\gamma(-\omega;\omega,\omega,-\omega)$ are given by the following sum-over-states expression:⁸³

$$\gamma_{ijkl}(-\omega;\omega,\omega,-\omega) = \frac{1}{\hbar^3} \sum_{lmn} \left\{ \frac{\langle g|\mu_i|l\rangle\langle l|\bar{\mu}_j|m\rangle\langle m|\bar{\mu}_k|n\rangle\langle n|\mu_l|g\rangle}{(\Omega_{lg} - \omega)(\Omega_{mg} - 2\omega)(\Omega_{ng} - \omega)} + \frac{\langle g|\mu_i|l\rangle\langle l|\bar{\mu}_i|m\rangle\langle m|\bar{\mu}_k|n\rangle\langle n|\mu_l|g\rangle}{(\Omega_{lg}^* - \omega)(\Omega_{mg} - 2\omega)(\Omega_{ng} - \omega)} + \frac{\langle g|\mu_i|l\rangle\langle l|\bar{\mu}_j|m\rangle\langle m|\bar{\mu}_i|n\rangle\langle n|\mu_l|g\rangle}{(\Omega_{lg} - \omega)(\Omega_{mg} - 2\omega)(\Omega_{ng} - \omega)} + \frac{\langle g|\mu_i|l\rangle\langle l|\bar{\mu}_j|m\rangle\langle m|\bar{\mu}_k|n\rangle\langle n|\mu_l|g\rangle}{(\Omega_{lg}^* - \omega)(\Omega_{mg} - 2\omega)(\Omega_{ng} - \omega)} \right\} \quad (12)$$

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where only TP resonant terms have been retained, g is the ground state, and the summation runs over all excited states; $\Omega_{1g} = \omega_{1g} - i\Gamma_{1g}$, and $\bar{\mu} = \mu - \langle g|\mu|g\rangle$. In our case, the only term different from 0 is the γ_{zzzz} term, where z is the axis in the D-A-D direction. The orientationally averaged second hyperpolarizability is thus given by $\langle \gamma \rangle = 1/5\gamma_{zzzz}$.⁸² Consistently with the Taylor expansion series for the polarizability, the expression in eq 12 is 6 times bigger than the expression that one would obtain when expanding the polarization in a perturbative series.⁸⁴

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